

Plotting Complex Functions

☒ pz —————
☐ Examples —————

`pZ("f", B, N, cm)` plots the argument of $f(z)$ in the box B with N points with the colormap cm

`cm := pCmapJet(200, 1)`

$$B := \begin{bmatrix} -6 & 6 \\ -3 & 3 \end{bmatrix} = \begin{bmatrix} x1 & x2 \\ y1 & y2 \end{bmatrix}$$

$$N := 2 \cdot \begin{bmatrix} 100 \\ 50 \end{bmatrix} = \begin{bmatrix} nx \\ ny \end{bmatrix}$$

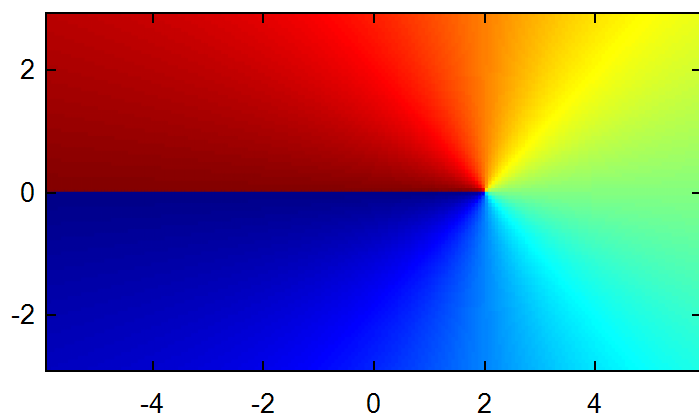
`pZ("f", B, N)` plots the complex map of $f(z)$ in the box B with N points

$$B' := B \quad N' := 1 \cdot \begin{bmatrix} 20 \\ 20 \end{bmatrix}$$

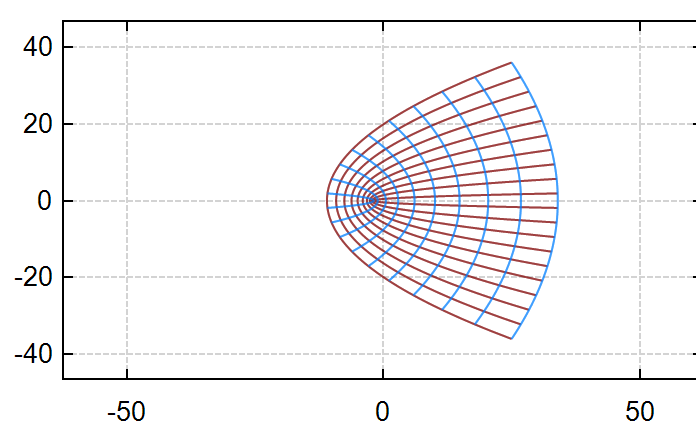
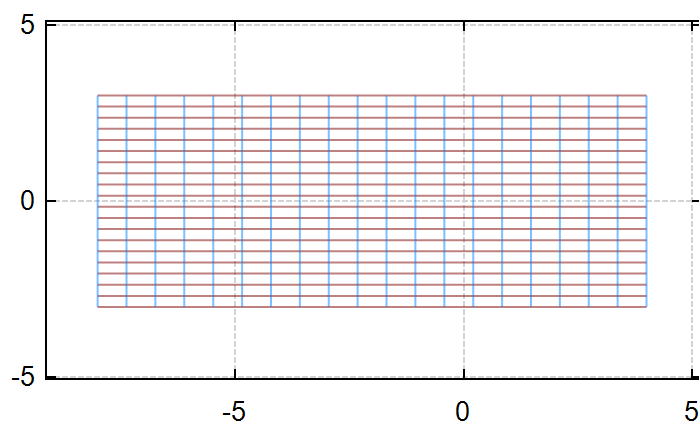
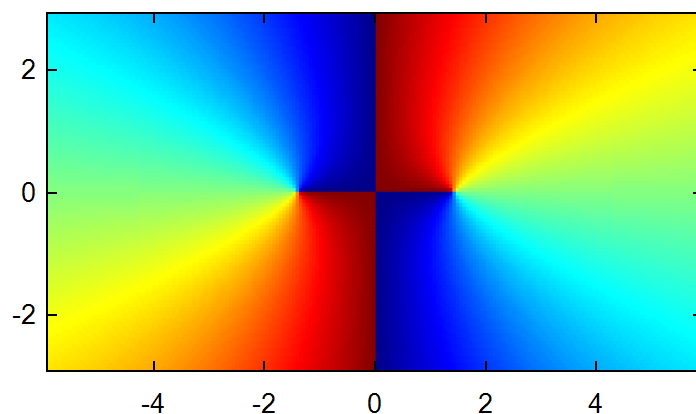
Zeros

counterclockwise color change. Also, the polynomial degree cycle the colors.

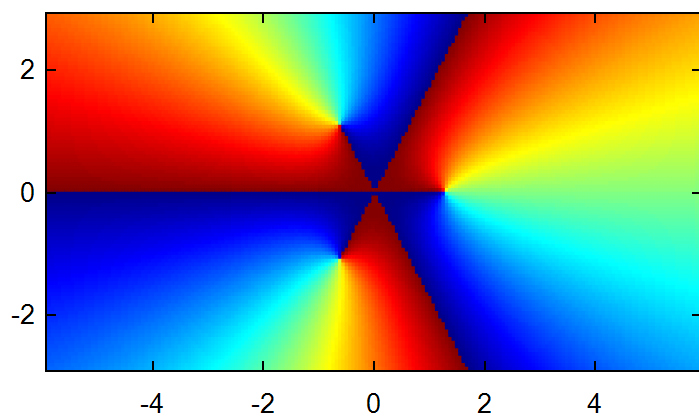
$$f_1(z) := z - 2$$



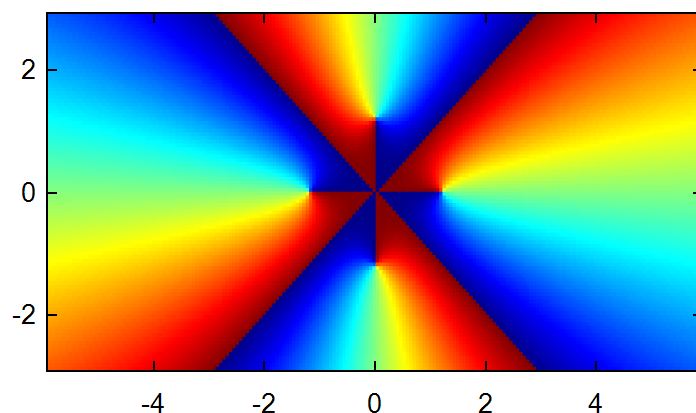
$$f_2(z) := z^2 - 2$$

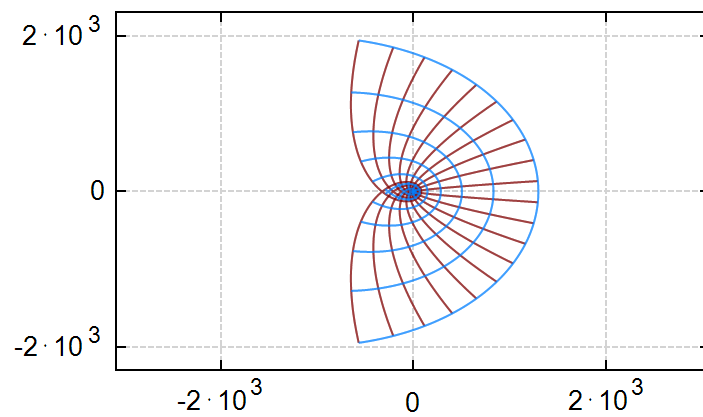
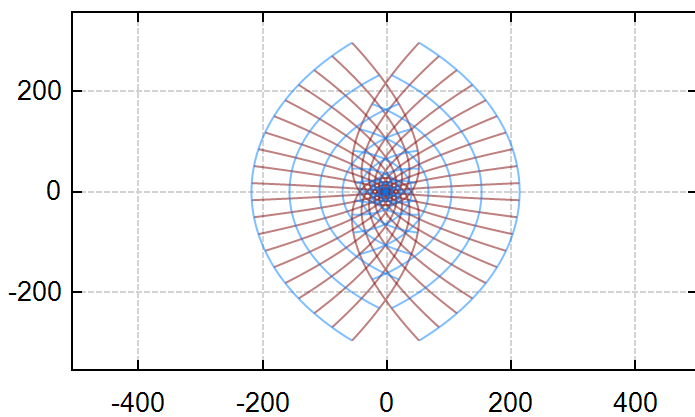


$$f_1(z) := z^3 - 2$$



$$f_2(z) := z^4 - 2$$

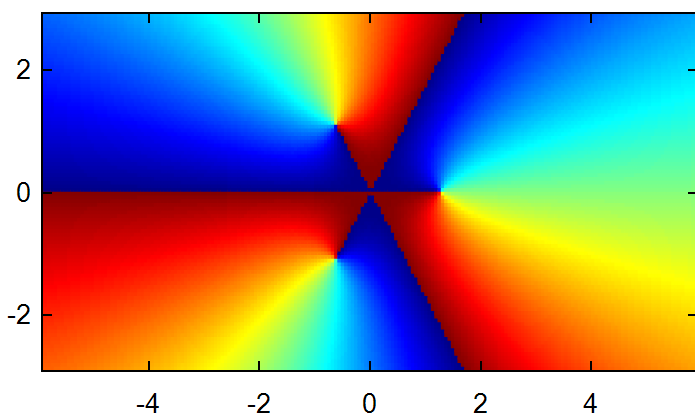




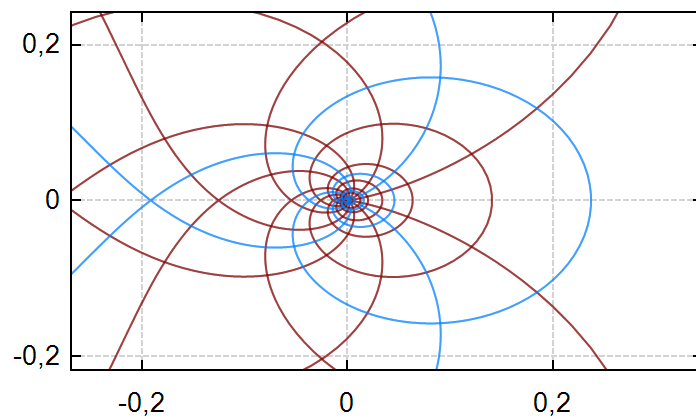
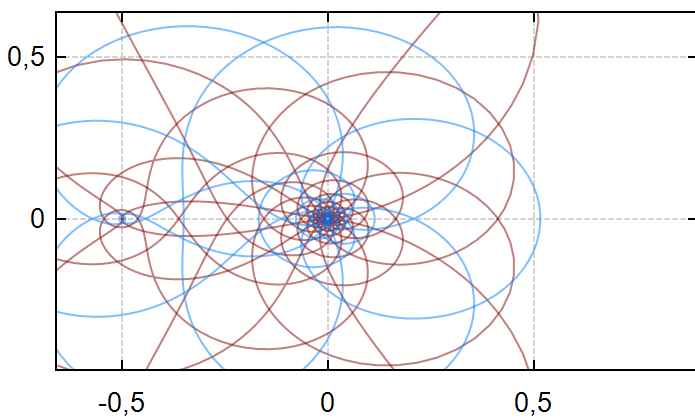
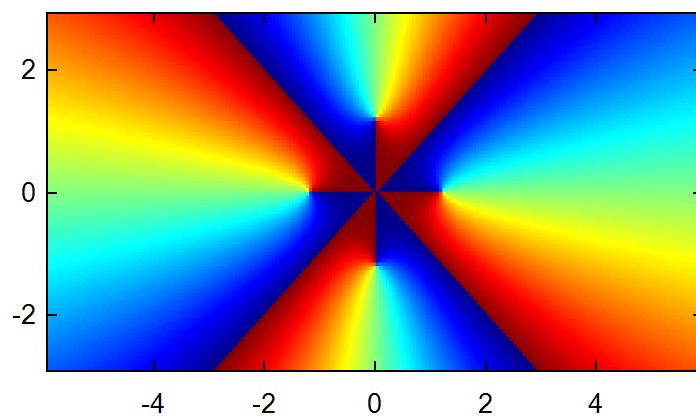
Poles

clockwise color change.

$$f_1(z) := \frac{1}{z^3 - 2}$$

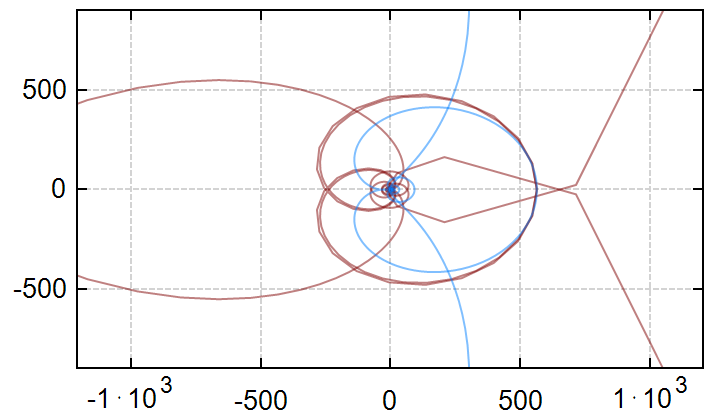
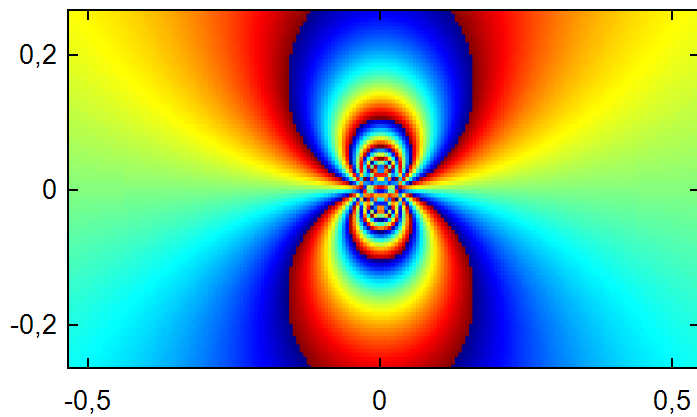


$$f_2(z) := \frac{1}{z^4 - 2}$$



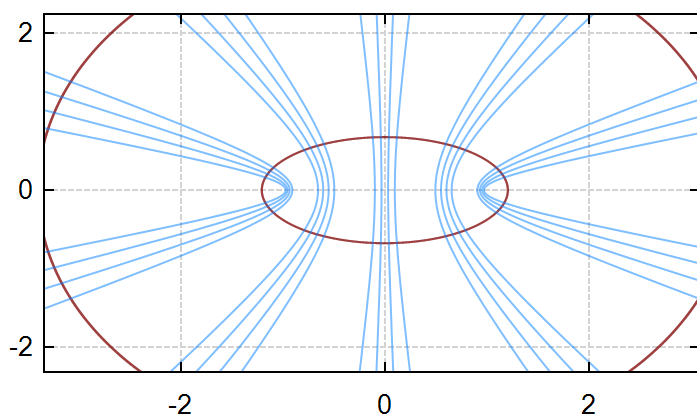
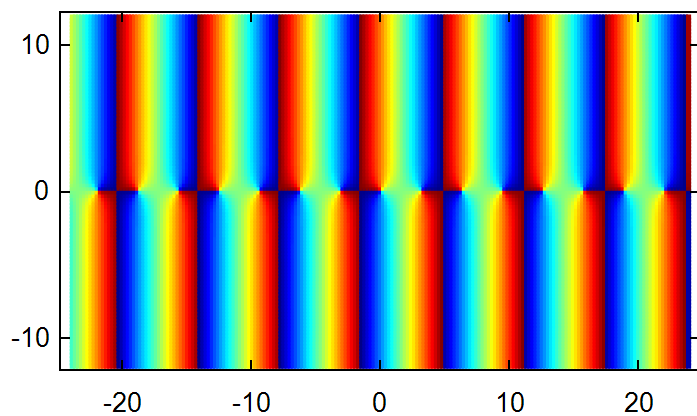
Essential discontinuity infinite color change.

$$f_1(z) := e^{-\frac{1}{z}}$$

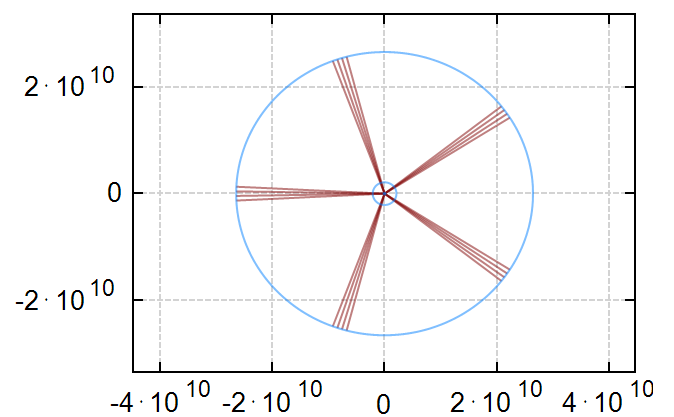
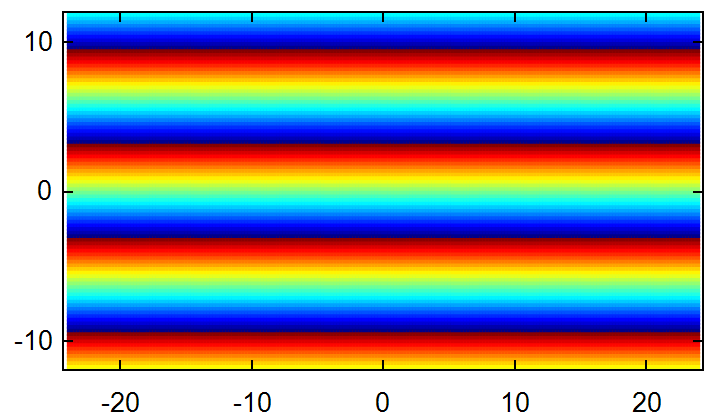


Periodicity

$$f_1(z) := \sin(z) \quad \text{period } 2\pi \text{ (horizontal)}$$

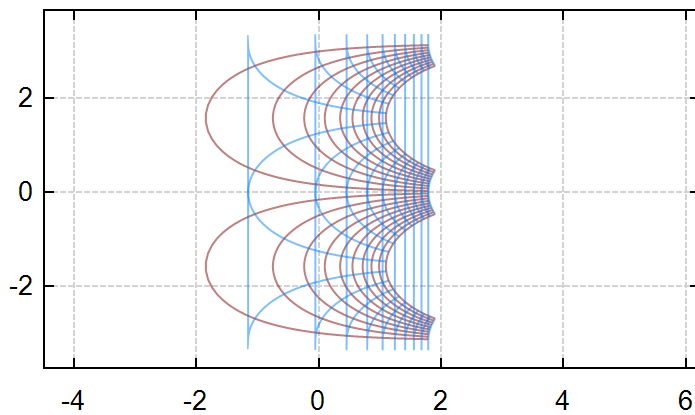
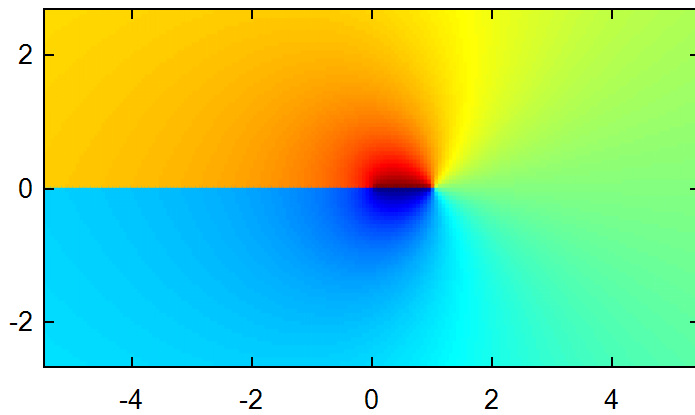


$$f_2(z) := e^z \quad \text{period } 2\pi i \text{ (vertical)}$$

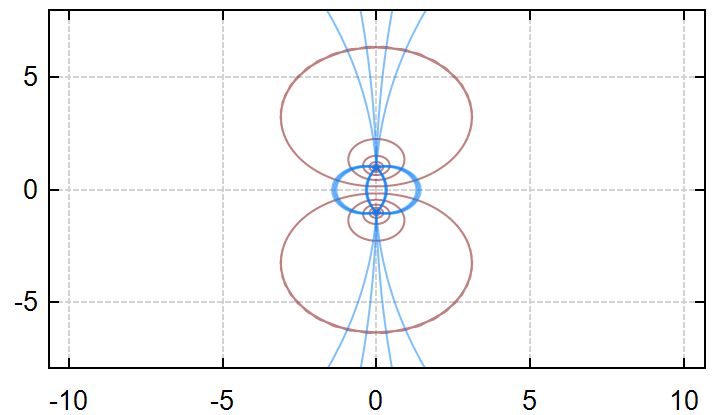
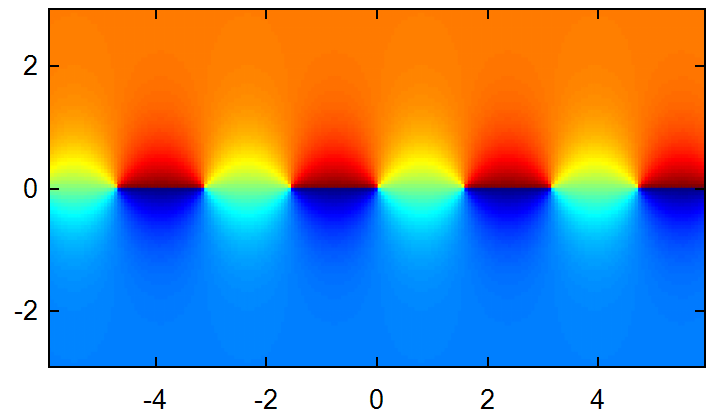


Gallery

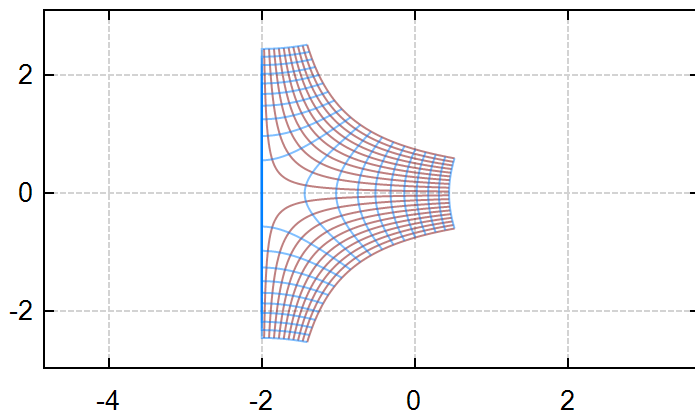
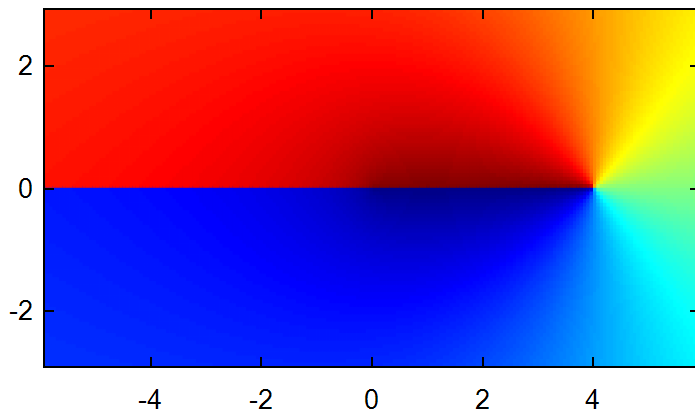
$$f_1(z) := \ln(z)$$



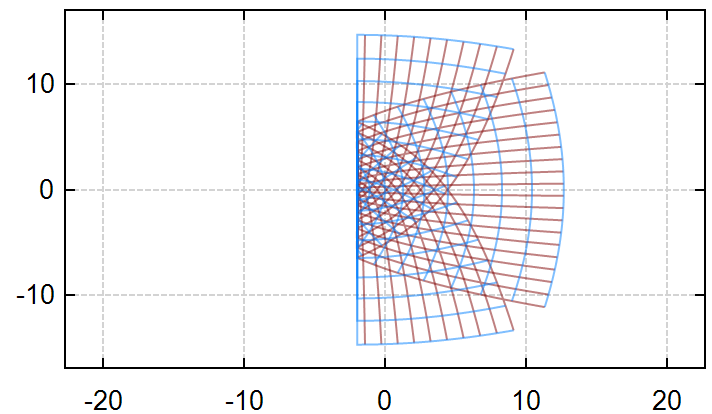
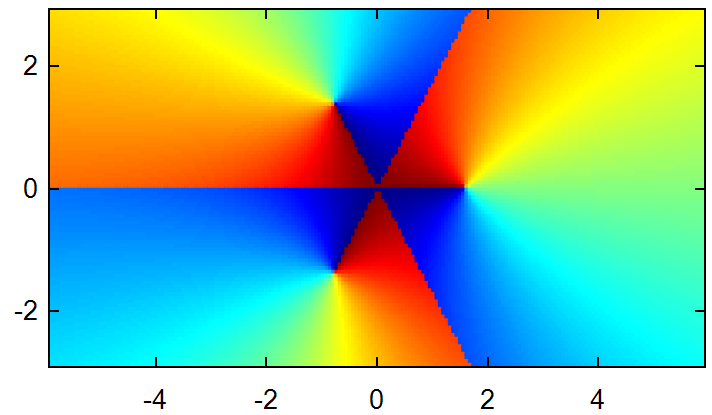
$$f_2(z) := \tan(z)$$



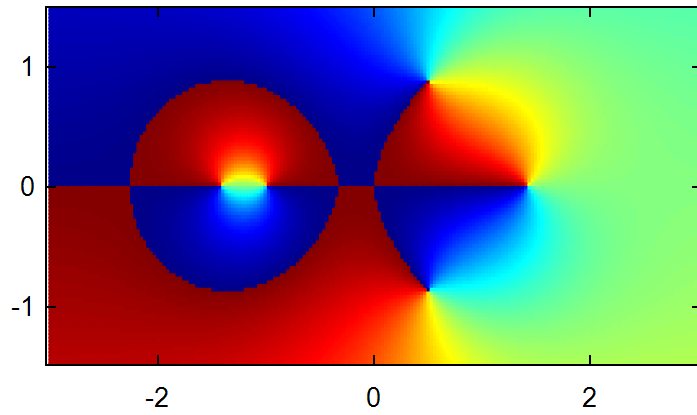
$$f_1(z) := \sqrt{z} - 2$$



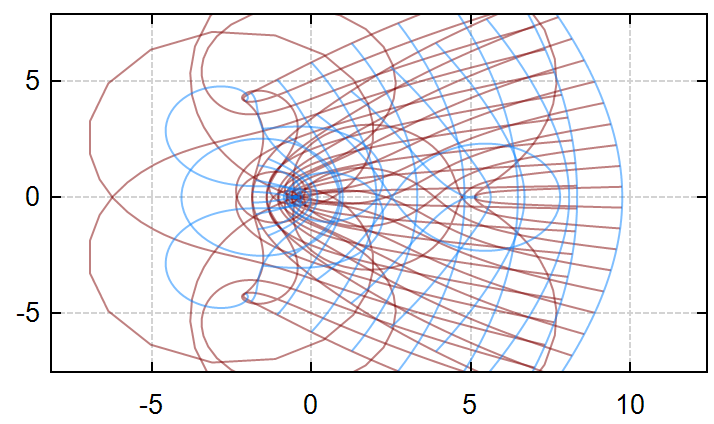
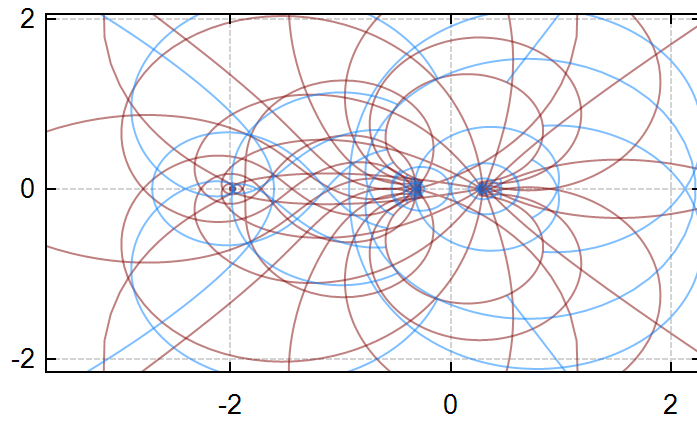
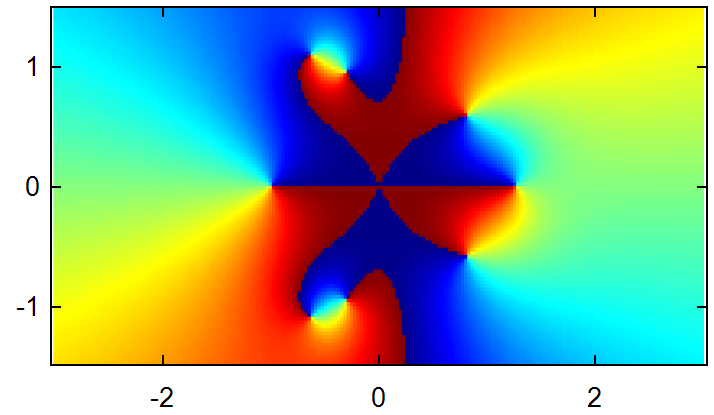
$$f_2(z) := \sqrt[3]{z} - 2$$



$$f_1(z) := \frac{z^2 - 2}{z^3 + 1}$$



$$f_2(z) := \frac{z^5 + 1}{z^3 - 2}$$



Alvaro