

Plotting Complex Functions

⊞ pz —

⊞ Examples —

`pZ("f", B, N, cm)` plots the argument of $f(z)$ in the box B with N points with the colormap cm

`cm := pCmapJet(200, 1)`

$$B := \begin{bmatrix} -6 & 6 \\ -3 & 3 \end{bmatrix} = \begin{bmatrix} x1 & x2 \\ y1 & y2 \end{bmatrix}$$

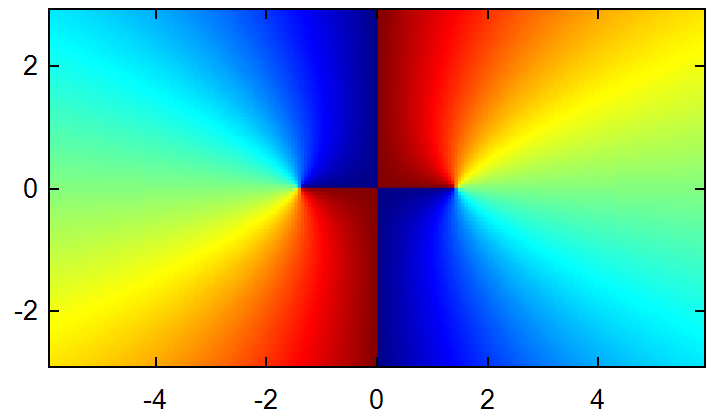
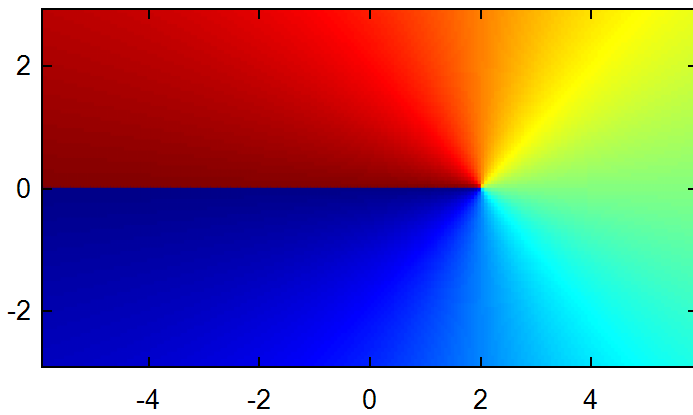
$$N := 2 \cdot \begin{bmatrix} 100 \\ 50 \end{bmatrix} = \begin{bmatrix} nx \\ ny \end{bmatrix}$$

Zeros

counterclockwise color change. Also, the polynomial degree cycle the colors.

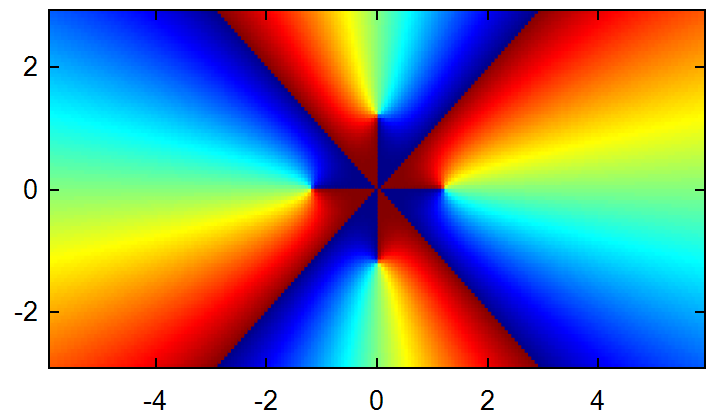
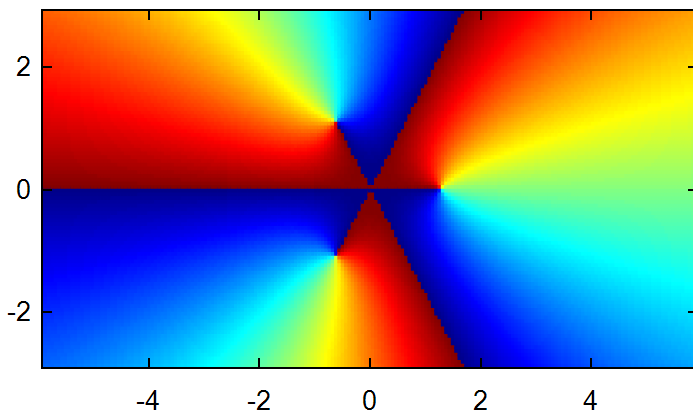
$$f_1(z) := z - 2$$

$$f_2(z) := z^2 - 2$$



$$f_1(z) := z^3 - 2$$

$$f_2(z) := z^4 - 2$$

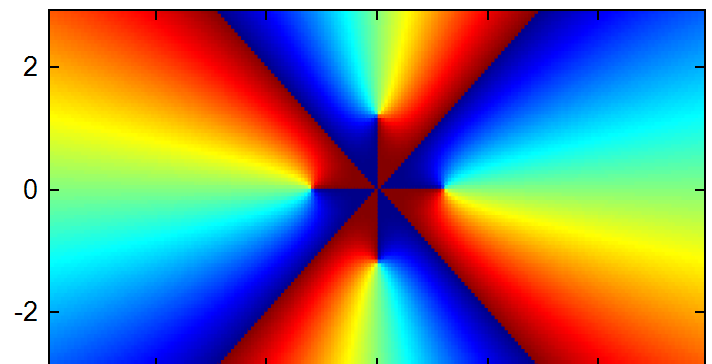
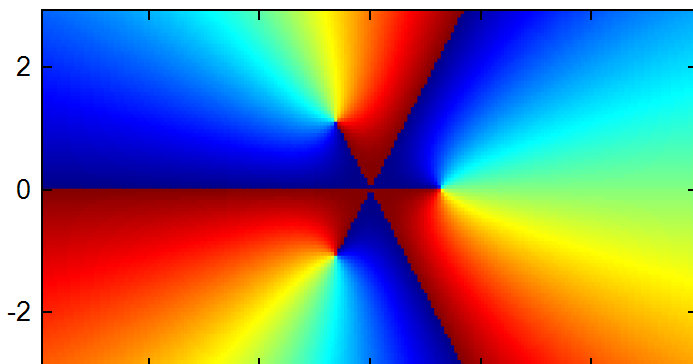


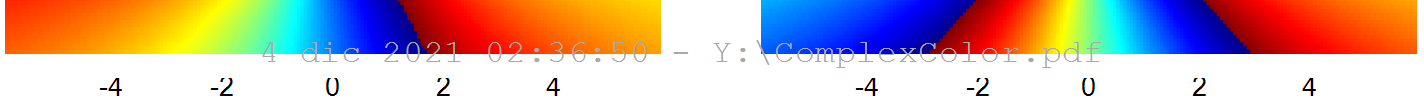
Poles

clockwise color change.

$$f_1(z) := \frac{1}{z^3 - 2}$$

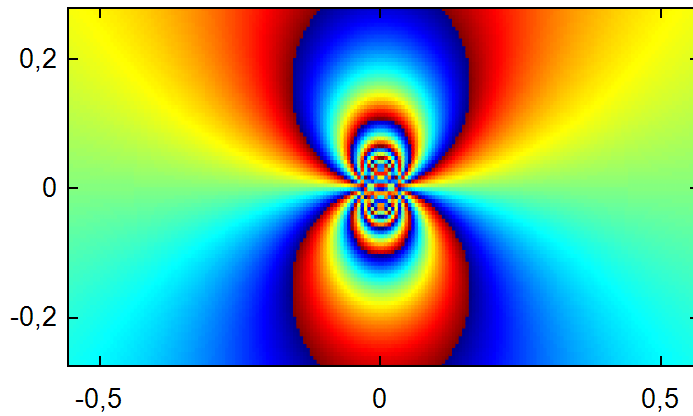
$$f_2(z) := \frac{1}{z^4 - 2}$$





Essential discontinuity infinite color change.

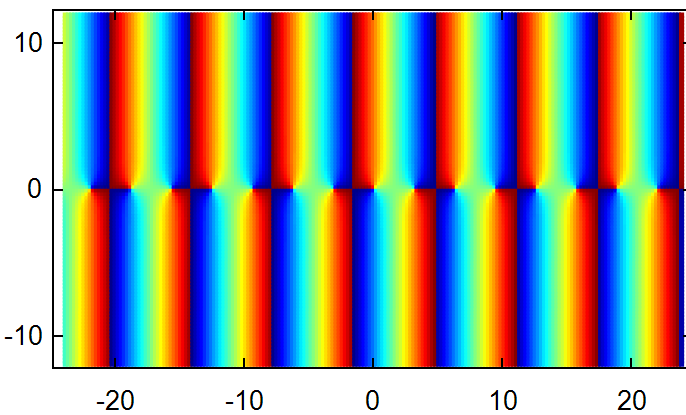
$$f_1(z) := e^{-\frac{1}{z}}$$



`pZ("f.1", 0.1*B, N, cm)`

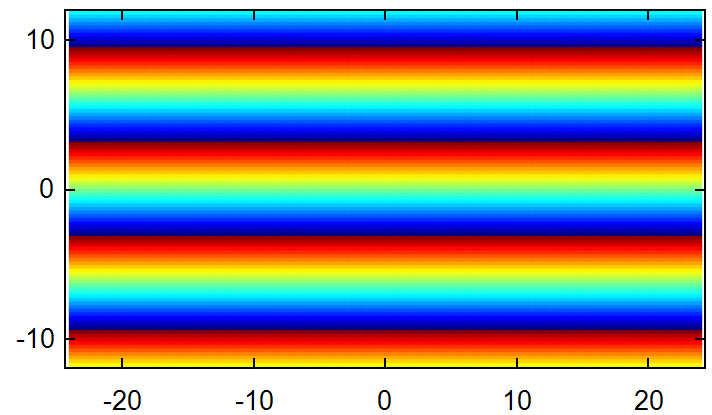
Periodicity

$$f_1(z) := \sin(z) \quad \text{period } 2\pi \text{ (horizontal)}$$



`pZ("f.1", 4*B, N, cm)`

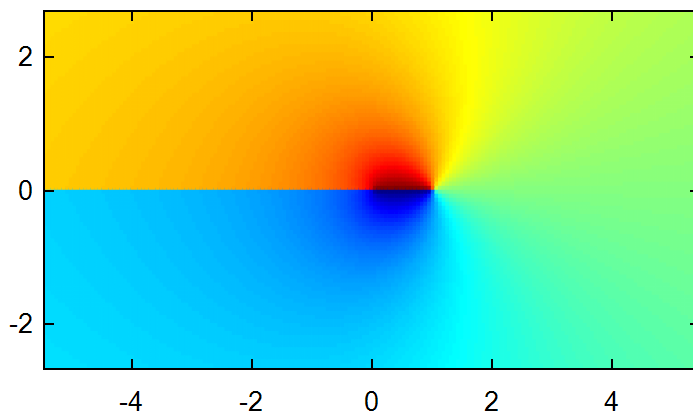
$$f_2(z) := e^z \quad \text{period } 2\pi i \text{ (vertical)}$$



`pZ("f.2", 4*B, N, cm)`

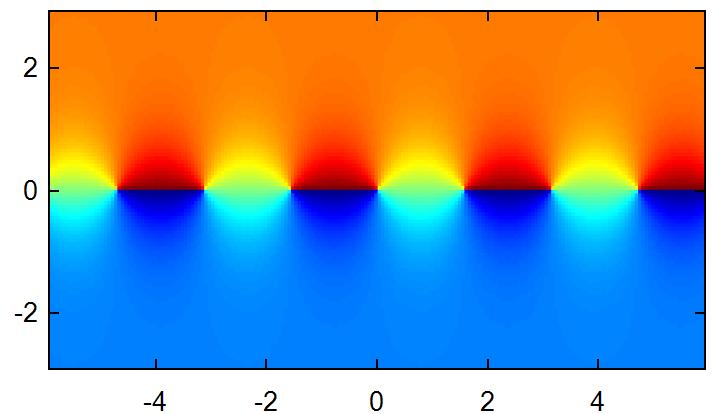
Gallery

$$f_1(z) := \ln(z)$$



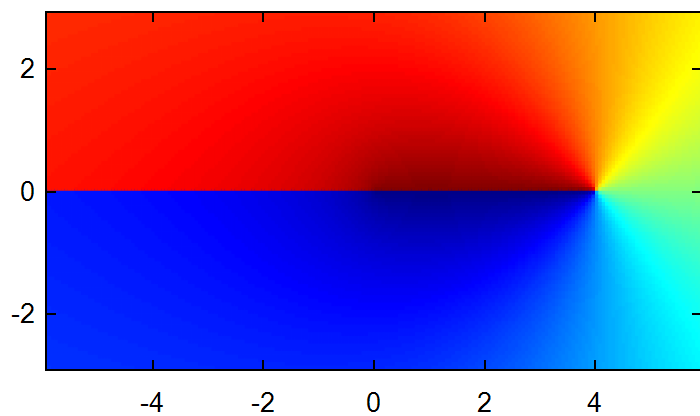
`pZ("f.1", B, N, cm)`

$$f_2(z) := \tan(z)$$



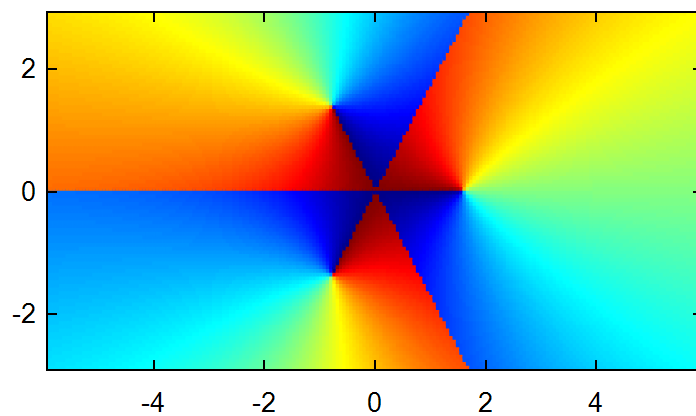
`pZ("f.2", B, N, cm)`

$$f_1(z) := \sqrt{z} - 2$$



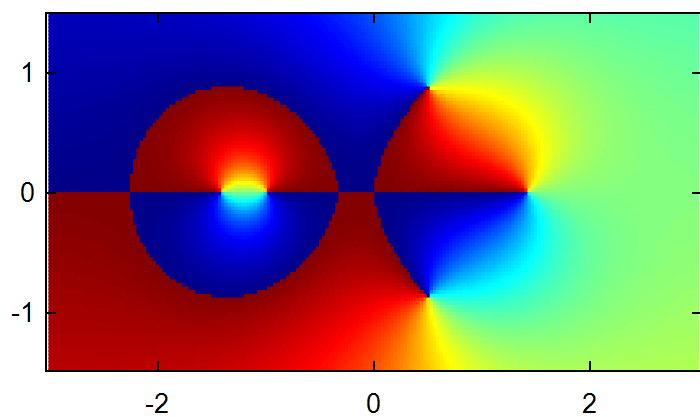
$pZ("f.1", B, N, cm)$

$$f_2(z) := \sqrt[3]{z} - 2$$



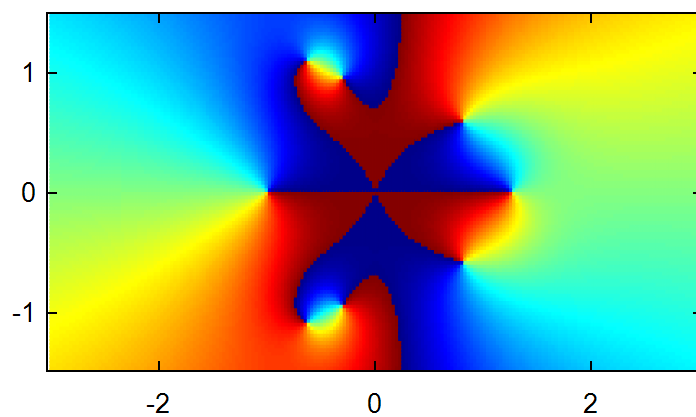
$pZ("f.2", B, N, cm)$

$$f_1(z) := \frac{z^2 - 2}{z^3 + 1}$$



$pZ("f.1", 0.5 \cdot B, N, cm)$

$$f_2(z) := \frac{z^5 + 1}{z^3 - 2}$$



$pZ("f.2", 0.5 \cdot B, N, cm)$

Alvaro