

Embedding images into a plot

	<code>img2xy</code>	
	<code>img2xy(M, ch, sz, a)</code>	Plots the image in M with characters ch with size sz and transparency color a into a native SMath plot
	<code>img2xy(M, a)</code>	Plots the image in M with transparency color a into a XY plot plugin

 Example: LogSpiral

Example: Logarithmic spiral

Nautilus shell `M:=image2rgb("Nautilus.jpg")` `Clear(a,b)=1`

Read this values from the graph

<code>xo:=68</code>	<code>yo:=89</code>	for	$O := \begin{bmatrix} x_o & y_o \end{bmatrix}$	$f(-\infty) = O$
<code>xa:=174</code>			$A := \begin{bmatrix} x_a & y_o \end{bmatrix}$	$f(0) = A$
<code>xb:=103</code>			$B := \begin{bmatrix} x_b & y_o \end{bmatrix}$	$f(2 \cdot \pi) = B$

Logarithmic spiral equation $f(t) := a \cdot b^t \cdot [\cos(t) - \sin(t)] + \begin{bmatrix} x_o & y_o \end{bmatrix}$

Solving numerically

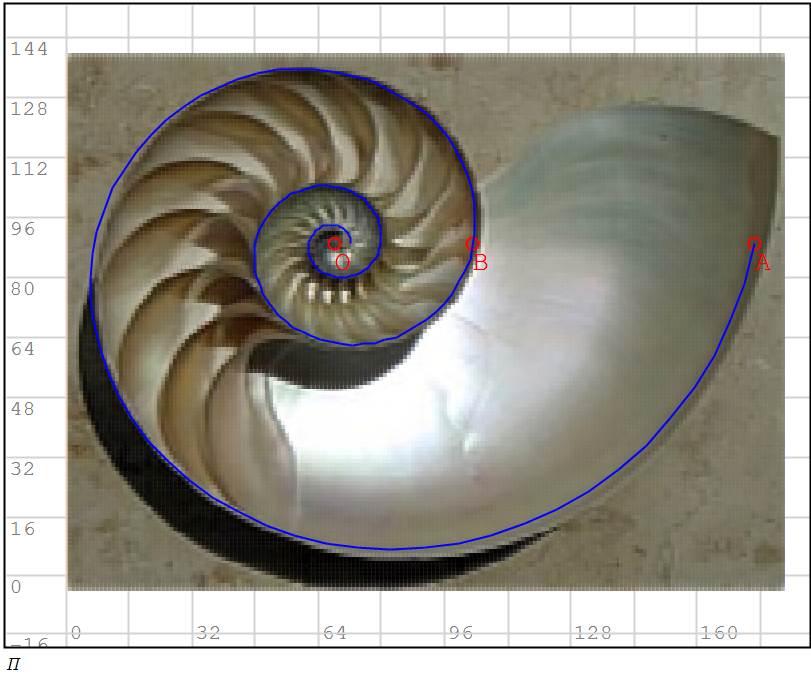
$a := \text{eval}\left(\text{roots}\left(\overrightarrow{f(0)}_1 - x_a, a\right)\right)$	$a = 106$
$b := \text{eval}\left(\text{roots}\left(\overrightarrow{f(2 \cdot \pi)}_1 - x_b, b, 1\right)\right)$	$b = 0.8383$

Or by hand

$f(0) = a \cdot \begin{bmatrix} 1 & 0 \end{bmatrix} + \begin{bmatrix} x_o & y_o \end{bmatrix} = \begin{bmatrix} x_a & y_o \end{bmatrix}$	thus	$a := x_a - x_o = 106$
$f(2 \cdot \pi) = a \cdot b^{2 \cdot \pi} \cdot \begin{bmatrix} 1 & 0 \end{bmatrix} + \begin{bmatrix} x_o & y_o \end{bmatrix} = \begin{bmatrix} x_b & y_o \end{bmatrix}$		$b := 2 \cdot \pi \sqrt{\frac{x_b - x_o}{a}} = 0.8383$

Plot in SMath

```
XY:=matrix(0,2)
for t ∈ [0,0.1..(6·π)]
  XY:=eval(stack(XY,f(t)))
Π:= {
  XY
  Point("A")
  Point("B")
  Point("O")
  img2xy(M,"",4,0.6)
```

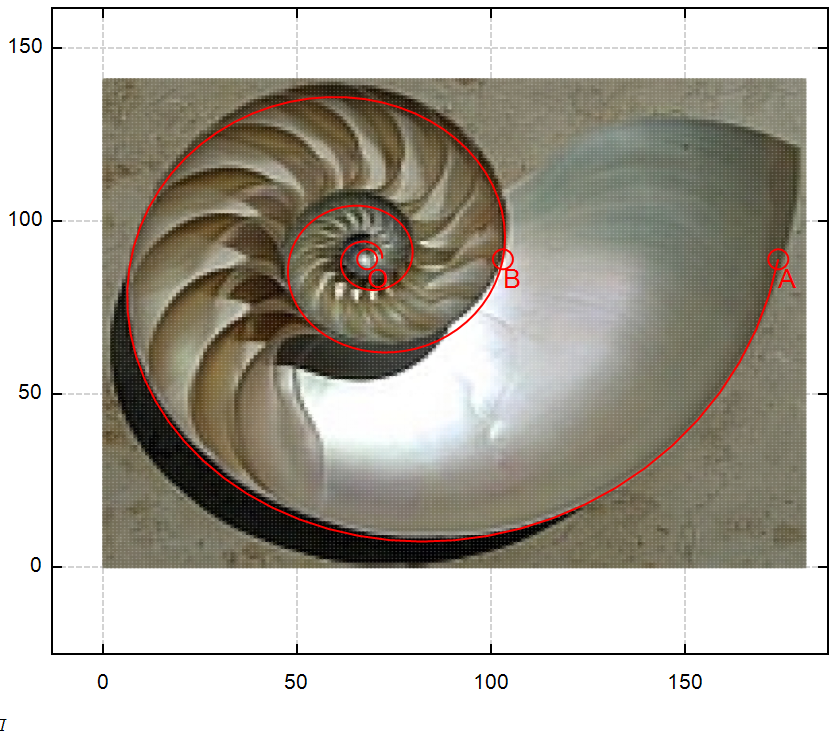


Plot in XY plugin.

```

Π := {
  img2xy (M, 0.8)
  Point ("A")
  Point ("B")
  Point ("O")
  XY
}
```

Image in this sample:



Π

Example: Catenary

Example: Catenary

We use here the grayscale of the image.

Budapest Keleti Railway Station

```

M := image2rgb ("Budapest_Keleti_teto.jpg")
GS := 1/3 * (Σ M)
```

Image
http

Read this points in the graph

```

A := [ 8 64 ]
O := [ 82 114 ]
```

Clear (a, xo, yo) = 1

Catenary equation

$f(x) := a \cdot \cosh\left(\frac{x - x_o}{a}\right) + y_o$ with $x_o := O_1$ $y_o := A_2 + O_2$

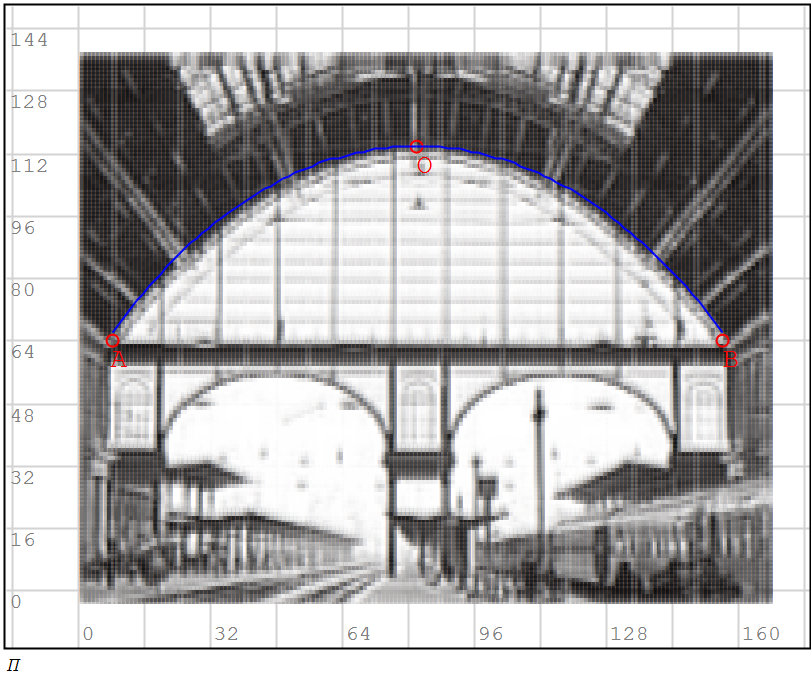
Find a

$a := \text{eval}\left(\text{roots}\left(f(O_1) = O_2, a, -50\right)\right) = -64$

Plot in SMath

```

B := [ 2 * O_1 - A_1 A_2 ]
X := A_1 + (B_1 - A_1) / 100 * [ 0 .. 100 ]
Π := {
  augment (X, f(X))
  Point ("A")
  Point ("B")
  Point ("O")
  img2xy (GS, " ", 4, 0.4)
}
```

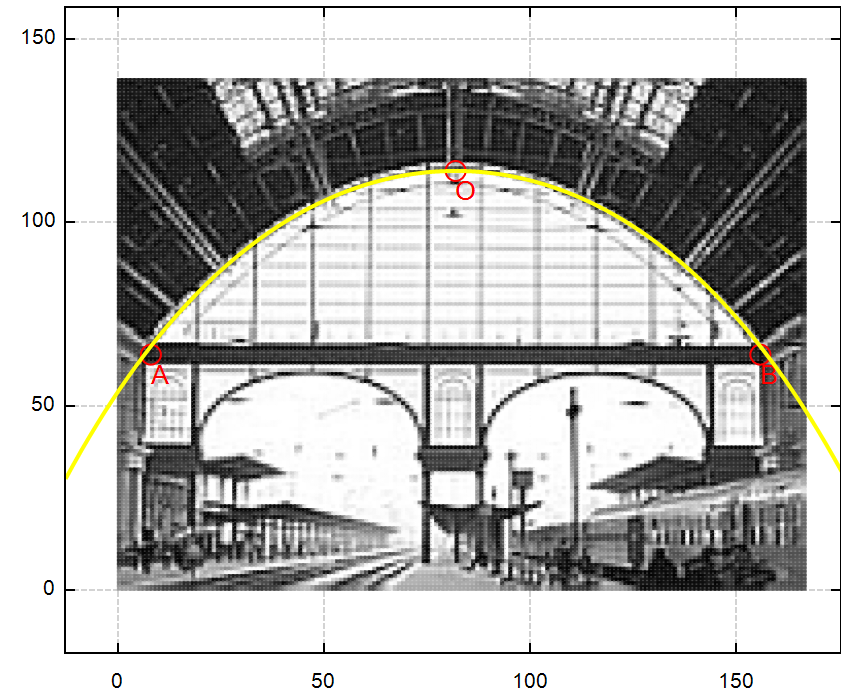


Π

Plot in XY plugin.

```

Π := {
  img2xy (GS, 0.8)
  Point ("A")
  Point ("B")
  Point ("O")
  f (x)
}
```



Π

Alvaro