

1. The Semenov Model<http://demonstrations.wolfram.com/TheSemenovModel/>

Semenov developed a model that describes the thermal ignition phenomenon quantitatively

Denote the

$$x_1 = \gamma \quad x_2 = T \quad \varepsilon := 0.15$$

where T is a dimensionless temperature, γ depends on the overall heat transfer coefficient, and ε depends on the activation energy

The dimensionless equation

$$f_1 := e^{-\frac{1}{\varepsilon \cdot x_2^2}} - x_1 \cdot (x_2 - 1) = 0$$

Coordinates of initial points

$$x_{0,1} := 0.1 \quad x_{0,2} := \text{solve}\left(e^{-\frac{1}{\varepsilon \cdot T}} - x_{0,1} \cdot (T - 1) = 0, T, 0, 15\right)$$

Dragilev's Method

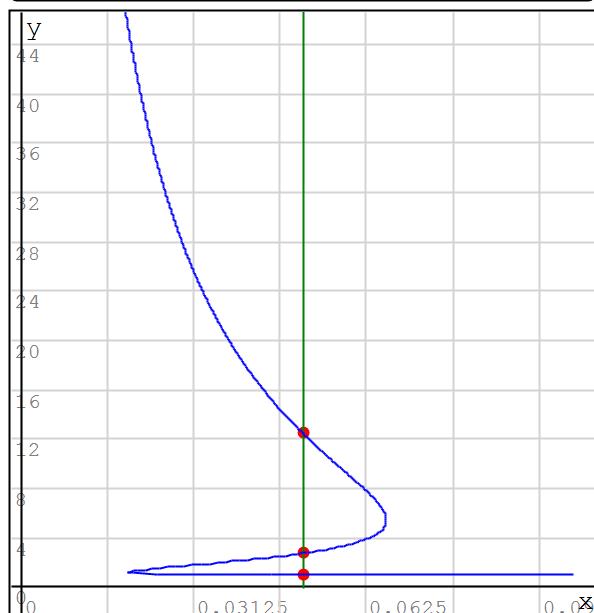
$$t_{\min} := 0 \quad t_{\max} := -48 \quad \Delta t := -0.06 \quad N := \frac{t_{\max}}{\Delta t} = 800$$

$$B := D(x_{0,1}, t_{\min}, t_{\max}, N) \quad \gamma(t) := 0.021 + 0.0025 \cdot t$$

$$T(t) := \begin{cases} \text{root} := \text{solve}\left(e^{-\frac{1}{\varepsilon \cdot y}} - \gamma(t) \cdot (y - 1) = 0, y, 0, 50\right) \\ T := \text{if } t > 18.8 \\ \quad \text{stack}(\text{root}, 100, 100) \\ \text{else} \\ \quad \text{root} \end{cases}$$

$$\tau := 0 \dots 28$$

Dependence T of on the parameter γ
The red dots show the stationary states



2. Continuously Stirred Tank Reactor

<http://demonstrations.wolfram.com/ContinuouslyStirredTankReactorUsingArcLengthParameter/>

x1-dimensionless concentration, x2-dimensionless temperature, Da-Damköhler number,
 γ -dimensionless activation energy, β -dimensionless heat transfer coefficient

$$B := 10 \quad Da := 0.03084 \quad \gamma := 20 \quad T_0 := -5$$

Denote the

$$x_1 = x \quad x_2 = T \quad x_3 = Da$$

Координаты начальных точек

$$x_{0,1} := 0.004 \quad x_{0,2} := -1.85 \quad x_{0,3} := 0.03084$$

$$t_{min} := 0 \quad t_{max} := -9.8 \quad \Delta t := -0.2 \quad N := \frac{t_{max}}{\Delta t}$$

The dimensionless equations

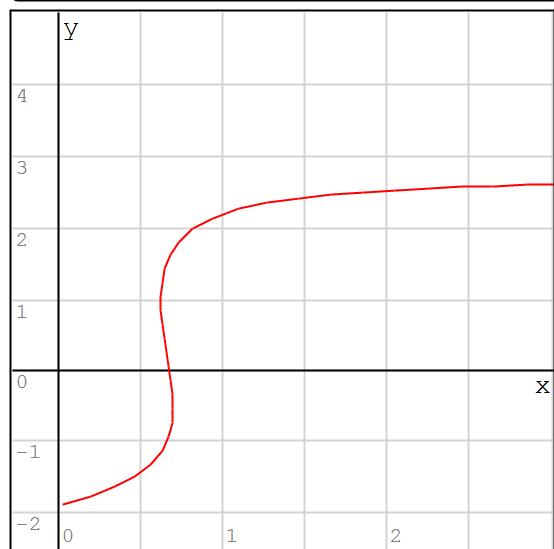
$$\begin{aligned} \varphi &:= -x_2 + B \cdot x_3 \cdot \left(1 - x_1\right) \cdot e^{-\frac{x_2}{\gamma}} \\ f_1 &:= -x_1 + x_3 \cdot \left(1 - x_1\right) \cdot e^{-\frac{x_2}{\gamma}} = 0 \end{aligned}$$

$$t_{start} := 6 \quad t_{end} := 30$$

$$\begin{aligned} \text{for } i \in t_{start} .. t_{end} \\ | \quad \beta_i := 0.2 + 0.04 \cdot i \\ | \quad f_2 := \varphi - \beta_i \cdot x_2 \\ | \quad K_i := D(x_0, t_{min}, t_{max}, N) \end{aligned}$$

$$\tau := t_{start} .. 2 \cdot t_{end} - t_{start}$$

Dependence T of on the parameter Da.
By increasing the heat transfer
coefficient the temperature drops



$$x_0 _1 := 1.496446999$$

$$x_0 _2 := -0.9574371296$$

$$x_0 _3 := 0$$