

**Problem:**

A rectangular channel (bottom width  $b$ , Manning's roughness coefficient  $n$ ) flows  $y_{norm}$  deep on a slope  $s$ .

A suppressed weir (height  $h_{weir}$ , weir coefficient  $C_{weir}$ ) is built across the channel.

Taking the elevation of the bottom of the channel just upstream from the weir to be  $z_B$ , estimate (using one reach) the elevation of the water surface at a point "A",  $H_A$ , which is  $L$  upstream from the weir. (See figure.)

**Given:**

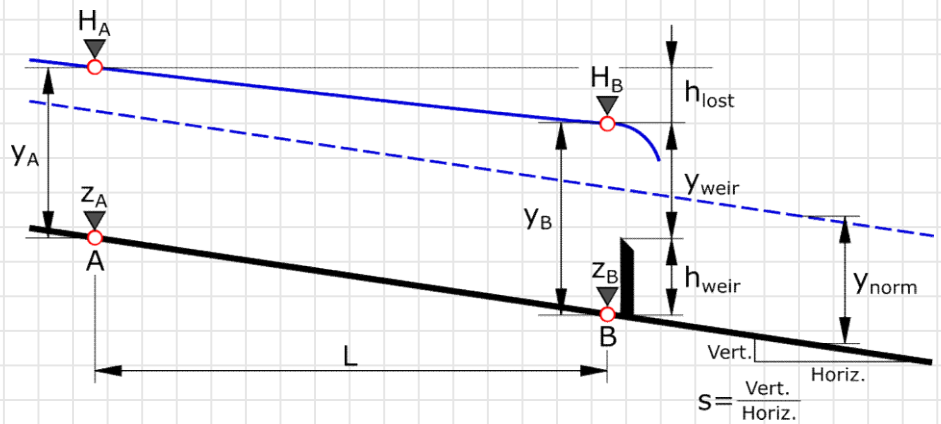
$$b = 20 \text{ ft} \quad n = 0.025 \frac{\text{s}}{\text{m}^{\frac{1}{3}}}$$

$$y_{norm} = 5 \text{ ft} \quad s = \frac{14.7}{10000}$$

$$z_B = 100 \text{ ft} \quad L = 1000 \text{ ft}$$

$$h_{weir} = 2.45 \text{ ft}$$

$$C_{weir} = 3.45 \frac{\text{ft}}{\text{s}^{\frac{1}{2}}}$$

**Solution:**

$$A = b \cdot y_{norm} = 100 \text{ ft}^2$$

$$p_w = b + 2 \cdot y_{norm} = 30 \text{ ft}$$

$$R = \frac{A}{p_w} = 3.3333 \text{ ft}$$

$$v = \frac{1}{n} \cdot R^{\frac{2}{3}} \cdot s^{\frac{1}{2}} = 5.0851 \frac{\text{ft}}{\text{s}}$$

$$Q = A \cdot v = 508.51 \frac{\text{ft}^3}{\text{s}}$$

$$y_B = 6.009 \text{ ft} \quad \text{estimated}$$

$$y_{weir} = y_B - h_{weir} = 3.559 \text{ ft}$$

$$v_B = \frac{Q}{b \cdot y_B} = 4.2312 \frac{\text{ft}}{\text{s}}$$

Flow over weir is given with following equation:

$$Q_{weir} = C_{weir} \cdot b \cdot \left[ \left( y_{weir} + \frac{v_B^2}{2g_e} \right)^{\frac{3}{2}} - \left( \frac{v_B^2}{2g_e} \right)^{\frac{3}{2}} \right] = 508.5249 \frac{\text{ft}^3}{\text{s}}$$

$$\Delta Q = Q - Q_{weir} = -0.0149 \frac{\text{ft}^3}{\text{s}} \quad \text{must be equal to zero} \quad \text{satisfactory enough, } y_B = 6.009 \text{ ft}$$

$$z_A = z_B + s \cdot L = 101.47 \text{ ft}$$

$$y_A = 5.43 \text{ ft} \quad \text{estimated}$$

$$A_A = b \cdot y_A = 108.6 \text{ ft}^2$$

$$v_A = \frac{Q}{A_A} = 4.6824 \frac{\text{ft}}{\text{s}}$$

$$v_{\text{average}} = \frac{1}{2} \cdot (v_A + v_B) = 4.4568 \frac{\text{ft}}{\text{s}}$$

$$R_{\text{average}} = \frac{\frac{1}{2} \cdot (y_A \cdot b + y_B \cdot b)}{\frac{1}{2} \cdot (b + 2 \cdot y_A + b + 2 \cdot y_B)} = 3.6385 \text{ ft}$$

$$h_{\text{lost}} = \left( \frac{\frac{v_{\text{average}} \cdot n}{\frac{2}{3}}}{R_{\text{average}}} \right)^2 \cdot L = 1.0047 \text{ ft}$$

Check Bernoulli's equation:

$$H_A = z_A + y_A = 106.9 \text{ ft}$$

$$H_B = z_B + y_B = 106.009 \text{ ft}$$

$$H_A - H_B - h_{\text{lost}} = -0.1137 \text{ ft}$$

must be equal to zero

satisfactory enough,  $y_A = 5.43 \text{ ft}$

$$\text{Thus: } H_A = 106.9 \text{ ft}$$