

Offset surface creation

pMesh

Case 1

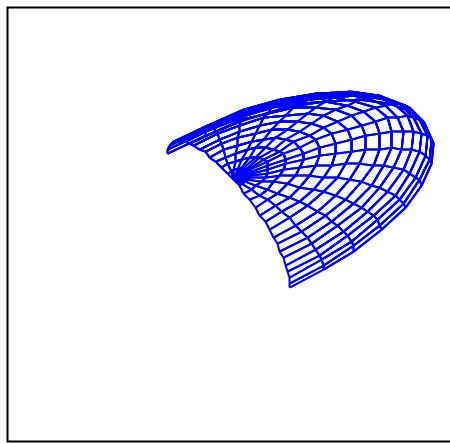
Solid between a surface and its displaced a fixed distance h in the direction of the surfaces normals

$$F_1(u, v) := \begin{bmatrix} 9 \cdot \sin(u) \cdot \cos(v) \\ 4.5 \cdot \sin(u) \cdot \sin(v) \\ 3 \cdot \cos(u) \end{bmatrix} \quad U_1 := pRange(0.5 \cdot \pi, 0, 16) + 0 \quad h_1 := 1$$

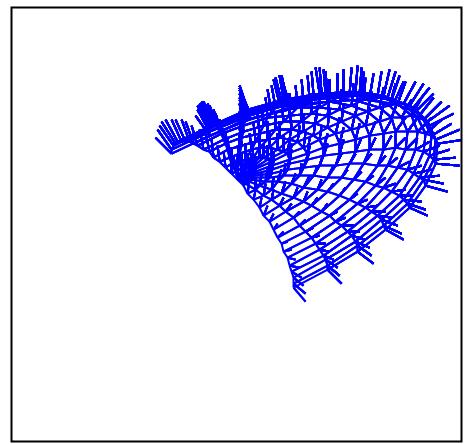
$$V_1 := pRange(1.5 \cdot \pi, 0.5 \cdot \pi, 16)$$

$$\begin{cases} M_1 := pMesh(F_1, U_1, V_1) \\ N_1 := pNo(F_1, U_1, V_1) \\ MN_1 := pNoMesh(M_1, N_1, h_1) \end{cases}$$

The surface

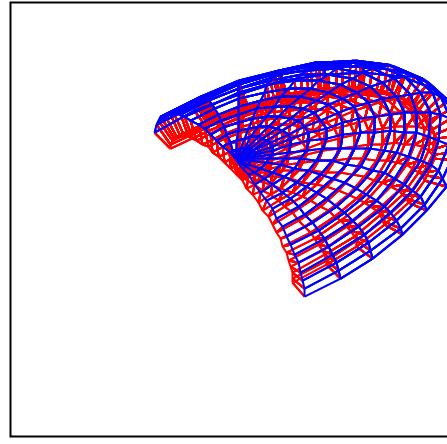
 $M_1 \cdot \gamma \cdot 1.2$

The surface with the normals

 $MN_1 \cdot \gamma \cdot 1.2$

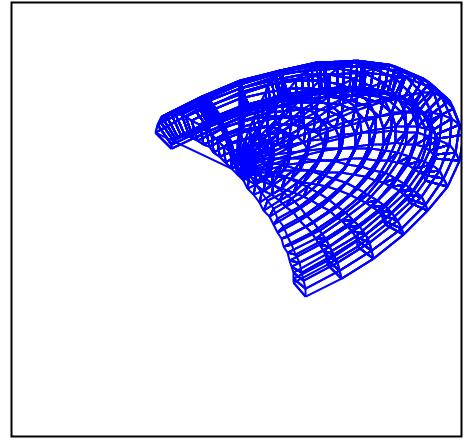
$$\begin{cases} M'_1 := M_1 + h_1 \cdot N_1 \\ A := \text{stack}(MN_1, M'_1) \end{cases}$$

Both together



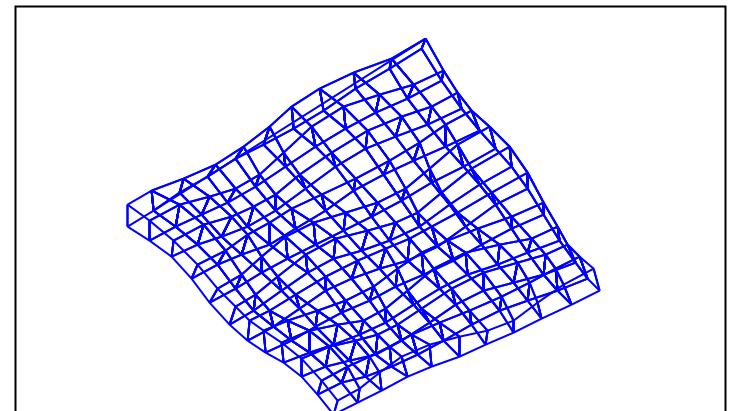
$$\begin{cases} M'_1 \cdot \gamma \cdot 1.2 \\ MN_1 \cdot \gamma \cdot 1.2 \end{cases}$$

The Solid as only one matrix

 $A \cdot \gamma \cdot 1.2$

Putting all together

$$\begin{cases} F_2(u, v) := \begin{bmatrix} u \\ v \\ 0.3 \cdot \sin(u) \cdot \cos(v) \end{bmatrix} \\ U_2 := pRange(-5, 5, 10) \\ V_2 := pRange(-5, 5, 11) \\ B := pNoSolid(F_2, U_2, V_2, 0.8) \end{cases}$$



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Case 2

Solid between a surface and its displaced a variable distance $h(u,v)$ in the direction of the surface normals

$$F_3(u, v) := \begin{bmatrix} u \\ v \\ \sin(0.5 \cdot u + 0.5 \cdot v) \end{bmatrix} \quad U_3 := pRange(-5, 5, 10) \quad h_3(u, v) := \sqrt{|u| + v}$$

$$V_3 := pRange(-5, 5, 10)$$

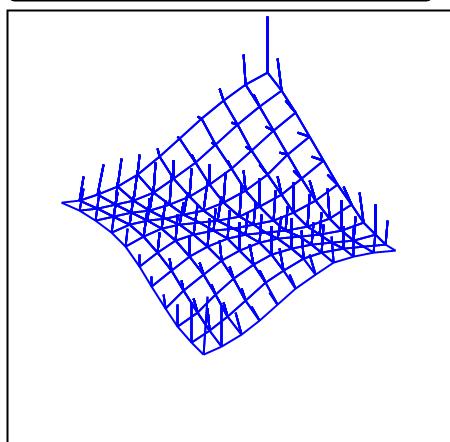
For generating the same structure for the scalar function h_3 we use the following cheat

$$H_3(u, v) := \text{matrix}(3, 1) + h_3(u, v)$$

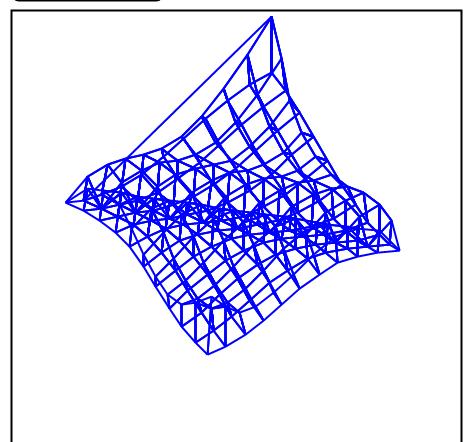
$$h_3 := pMesh("H.3", U_3, V_3)$$

$$\begin{aligned} M_3 &:= pMesh(F_3, U_3, V_3) \\ N_3 &:= pNo(F_3, U_3, V_3) \\ MN_3 &:= pNoMesh(M_3, N_3, h_3) \\ M'3 &:= \overrightarrow{M_3 + h_3 \cdot N_3} \\ C &:= \text{stack}(MN_3, M'3) \end{aligned}$$

The surface with the normals

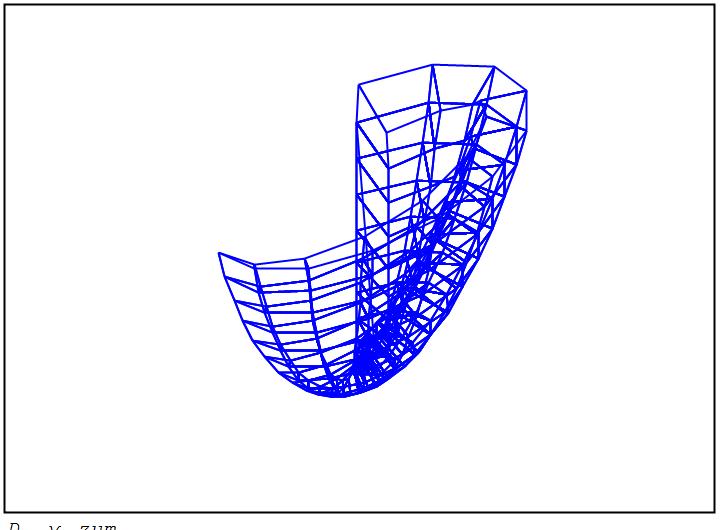


The Solid



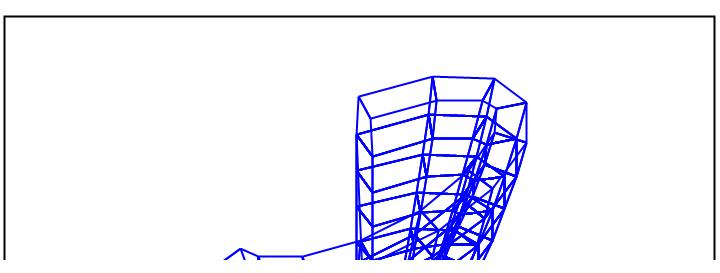
Putting all together

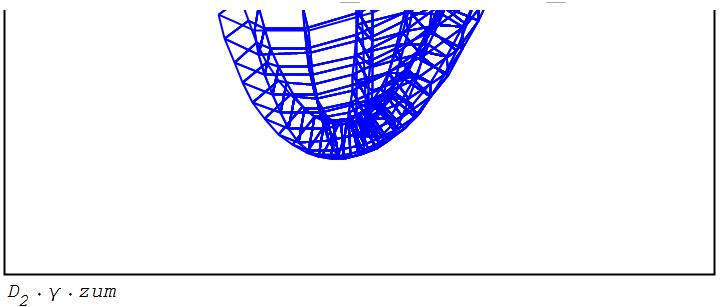
$$\begin{aligned} h_4(u, v) &:= 0.5 \cdot v \\ F_4(u, v) &:= \begin{bmatrix} 2 \cdot u \cdot \cos(v) \\ 1 \cdot u \cdot \sin(v) \\ u^2 - 5 \end{bmatrix} \\ U_4 &:= pRange(0.3, 3, 10) \\ V_4 &:= pRange(1.4 \cdot \pi, 0, 10) \\ D_1 &:= pNoSolid(F_4, U_4, V_4, h_4) \end{aligned}$$



Compare it with the "not distorted" solid

$$D_2 := pNoSolid(F_4, U_4, V_4, 1)$$





$D_2 \cdot Y \cdot \text{zum}$
